"Cotangent Bundles with General Natural Kahler Structures". By Simona Druta

Abstract: We study the conditions under which an almost Hermitian structure (G,J) of general natural lift type on the cotangent bundle T*M of a Riemannian manifold (M,g) is Kählerian. First, we obtain the algebraic conditions under which the manifold (T*M,G,J) is almost Hermitian. Next we get the integrability conditions for the almost complex structure J, then the conditions under which the associated 2-form is closed. The manifold (T*M,G,J) is Kählerian iff it is almost Kählerian and the almost complex structure J is integrable. It follows that the family of Kählerian structures of above type on T*M depends on three essential parameters (one is a certain proportionality factor, the next two are parameters involved in the definition of J). The final theorem gives the condition under which the Kählerian manifold (T*M,G,J) of general natural lift type has constant holomorphic sectional curvature.